

Name: *Key*

Date:

Hour:

Algebra 1
Unit 1 Review

Simplify each radical expression.

1. $-2\sqrt{24}$

$$\begin{array}{c} \uparrow \quad \uparrow \\ 4 \quad 6 \\ \uparrow \quad \uparrow \\ 2 \quad 2 \quad 3 \\ \hline -4\sqrt{6} \end{array}$$

2. $6\sqrt{54}$

$$\begin{array}{c} \uparrow \quad \uparrow \\ 6 \quad 9 \\ \uparrow \quad \uparrow \\ 2 \quad 3 \quad 3 \\ \hline 18\sqrt{6} \end{array}$$

3. $\sqrt{72}$

$$\begin{array}{c} \uparrow \quad \uparrow \\ 8 \quad 9 \\ \uparrow \quad \uparrow \\ 2 \quad 4 \quad 3 \quad 3 \\ \uparrow \quad \uparrow \\ 2 \quad 2 \\ \hline 6\sqrt{2} \end{array}$$

4. Solve for x: $4(x - 2) + 6x = 12 + 5x$.

$$\begin{array}{r} 4x - 8 + 6x = 12 + 5x \\ 10x - 8 = 12 + 5x \\ -5x \quad -5x \\ \hline 5x - 8 = 12 \\ +8 \quad +8 \\ \hline 5x = 20 \\ \frac{5x}{5} = \frac{20}{5} \\ \hline x = 4 \end{array}$$

5. Write and solve an equation to represent the following:
The difference of twice a number and 4 is 8

$$\begin{array}{r} 2x - 4 = 8 \\ +4 \quad +4 \\ \hline 2x = 12 \\ \frac{2x}{2} = \frac{12}{2} \\ \hline x = 6 \end{array}$$

Solve each equation.

6. $3(2x - 5) = 2(3x - 2)$

$$\begin{array}{r} 6x - 15 = 6x - 4 \\ -6x \quad -6x \\ \hline -15 = -4 \\ \text{no solution} \\ \emptyset \end{array}$$

7. $4x - 3 = 2x + 5$

$$\begin{array}{r} 4x - 3 = 2x + 5 \\ -2x \quad -2x \\ \hline 2x - 3 = 5 \\ +3 \quad +3 \\ \hline 2x = 8 \\ \frac{2x}{2} = \frac{8}{2} \\ \hline x = 4 \end{array}$$

8. $\frac{2}{3}x - 6 = \frac{4}{5}$

$$\begin{array}{r} \frac{2}{3}x - 6 = \frac{4}{5} \\ +6 \quad +6 \\ \hline \frac{2}{3}x = \frac{34}{5} \\ \frac{2x}{3} \times \frac{34}{5} \\ \hline \frac{10x}{10} = \frac{102}{10} \\ \hline x = \frac{51}{5} \end{array}$$

9. On the first day of the year, Alicia has \$1000 in her savings account and started spending \$25 a week. Her sister Kelsey had \$650 in her savings account and started saving \$15 a week. After how many weeks will the sisters have the same amount? What will that amount be?

$$\begin{array}{r}
 1000 - 25x = 650 + 15x \\
 +25x \qquad +25x \\
 \hline
 1000 = 650 + 40x \\
 -650 \quad -650 \\
 \hline
 350 = 40x
 \end{array}$$

$$\begin{array}{r}
 350 = 40x \\
 \frac{350}{40} = \frac{40x}{40} \\
 8.75 = x
 \end{array}$$

8.75 weeks
 $650 + 15(8.75)$
 $\$781.25$

10. Solve the equation. Write a justification for each step.

Statements	Reasons
$25 = 5(x - 3)$ $25 = 5x - 15$ $+15 \quad +15$	given Dist. POE Add POE
$\frac{40}{5} = \frac{5x}{5}$	Simplify Div POE
$8 = x$	Simplify

Solve each inequality. Then graph.

11. $-125 \geq 8p - 5$

$$\begin{array}{r}
 +5 \qquad +5 \\
 \hline
 -120 \geq 8p \\
 \frac{-120}{8} \geq \frac{8p}{8} \\
 -15 \geq p
 \end{array}$$

$p \leq -15$

12. $9 + \frac{x}{3} > 13$

$$\begin{array}{r}
 -9 \qquad -9 \\
 \hline
 3 \cdot \frac{x}{3} > 4 \cdot 3 \\
 x > 12
 \end{array}$$

$x > 12$

13. $98 < 7(3x + 5)$

$$\begin{array}{r}
 98 < 21x + 35 \\
 -35 \qquad -35 \\
 \hline
 63 < 21x \\
 \frac{63}{21} < \frac{21x}{21} \\
 3 < x
 \end{array}$$

$x > 3$

14. $-5(n + 1) - 6n \leq 83$

$$\begin{array}{r}
 -5n - 5 - 6n \leq 83 \\
 -11n - 5 \leq 83 \\
 +5 \qquad +5 \\
 \hline
 -11n \leq 88 \\
 \div \text{ by } -11 \text{ (negative)} \\
 n \geq -8
 \end{array}$$

$n \geq -8$

15. $6x - 5(8 - 5x) < 16 + 3x$

$$\begin{array}{r}
 6x - 40 + 25x < 16 + 3x \\
 31x - 40 < 16 + 3x \\
 -3x \qquad -3x \\
 \hline
 28x - 40 < 16 \\
 +40 \qquad +40 \\
 \hline
 28x < 56 \\
 \frac{28x}{28} < \frac{56}{28} \\
 x < 2
 \end{array}$$

$x < 2$

16. $3(x + 1) \geq 2(-2 + x)$

$$\begin{array}{r}
 3x + 3 \geq -4 + 2x \\
 -2x \qquad -2x \\
 \hline
 x + 3 \geq -4 \\
 -3 \qquad -3 \\
 \hline
 x \geq -7
 \end{array}$$

$x \geq -7$

Solve each compound inequality and graph its solution.

17. $33 > -8x - 7 \geq -79$

$$\begin{array}{r} 33 > -8x - 7 \\ +7 \quad +7 \\ \hline 40 > -8x \\ -8 \quad -8 \\ \hline -5 < x \end{array} \quad \begin{array}{r} -8x - 7 \geq -79 \\ +7 \quad +7 \\ \hline -8x \geq -72 \\ -8 \quad -8 \\ \hline x \leq 9 \end{array}$$

$-5 < x \leq 9$

19. $-7x + 7 > 42$ or $2 - x \leq -2$

$$\begin{array}{r} -7x + 7 > 42 \\ -7 \quad -7 \\ \hline -7x > 35 \\ -1 \quad -1 \\ \hline x < -5 \end{array} \quad \begin{array}{r} 2 - x \leq -2 \\ -2 \quad -2 \\ \hline -x \leq -4 \\ -1 \quad -1 \\ \hline x \geq 4 \end{array}$$

$x < -5$ or $x \geq 4$

21. A number x is more than -6 and at most 8 . Write this sentence as an inequality. Graph the solutions.

$-6 < x \leq 8$

22. You start a small baking business, and you want to earn a profit of at least \$250 in the first month. The expenses in the first month are \$155. Write and solve an inequality to represent the possible revenues that you need to earn to meet the profit goal?

$$\begin{array}{r} -155 + x \geq 250 \\ +155 \quad +155 \\ \hline x \geq 405 \end{array}$$

$x \geq 405$

23. Your monthly budget allows you to spend between \$200 and \$450, inclusively. You have already spent \$125. Write and solve a compound inequality to represent how much more money you have to spend for the rest of the month.

$$200 \leq x + 125 \leq 450$$

$$\begin{array}{r} 200 \leq x + 125 \\ -125 \quad -125 \\ \hline 75 \leq x \end{array} \quad \begin{array}{r} x + 125 \leq 450 \\ -125 \quad -125 \\ \hline x \leq 325 \end{array}$$

$75 \leq x \leq 325$

18. $-15 < -3(x - 2) < 33$

$$\begin{array}{r} -15 < -3(x - 2) \\ -6 \quad -6 \\ \hline -21 < -3x \\ -3 \quad -3 \\ \hline 7 > x \end{array} \quad \begin{array}{r} -3x + 6 < 33 \\ -6 \quad -6 \\ \hline -3x < 27 \\ -3 \quad -3 \\ \hline x > -9 \end{array}$$

$-7 < x < 7$

20. $8x - 4 \geq 20$ or $5x - 1 \leq 4$

$$\begin{array}{r} 8x - 4 \geq 20 \\ +4 \quad +4 \\ \hline 8x \geq 24 \\ 8 \quad 8 \\ \hline x \geq 3 \end{array} \quad \begin{array}{r} 5x - 1 \leq 4 \\ +1 \quad +1 \\ \hline 5x \leq 5 \\ 5 \quad 5 \\ \hline x \leq 1 \end{array}$$

$x \geq 3$ or $x \leq 1$

Simplify each.

24. $2x^4 \cdot 3x^{-1}$

$$\boxed{6x^3}$$

25. $\frac{x}{4x^{-1}}$

$$\boxed{\frac{x^2}{4}}$$

26. $x^3 \cdot 4x^3$

$$\boxed{4x^6}$$

27. $3x^0 \cdot x^2 y^3$

$$\boxed{3x^2 y^3}$$

28. $\frac{3x^{-3}}{3x^{-4}}$

$$\boxed{x}$$

29. $\frac{n^{-1}}{4n^2}$

$$\boxed{\frac{1}{4n^3}}$$

30. $\frac{2r}{r^3}$

$$\boxed{\frac{2}{r^2}}$$

31. $\frac{2a^{-4}}{a^{-3}}$

$$\boxed{\frac{2}{a}}$$