

ADVANCED GEOMETRY CHAPTER 3 REVIEW

BE SURE TO:

*Read the directions carefully and answer what the question is asking

*If you get stuck, look back to the section in your notes the problem comes from. This is probably a hint that you should spend more time studying this section.

3.5-3.6 Slope and Linear Equations

Find the missing variable.

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

1) $(x, -4), (7, 6)$ when the slope is $5/2$

$$\frac{6 + 4}{7 - x} = \frac{5}{2}$$

$$\frac{10}{7 - x} = \frac{5}{2}$$

$$\begin{aligned} 2(10) &= 5(7 - x) \\ 20 &= 35 - 5x \\ -15 &= -5x \\ 3 &= x \end{aligned}$$

2) $(-22, -4), (-12, y)$ when the slope is $3/5$

$$\frac{y + 4}{-12 + 22} = \frac{3}{5}$$

$$\frac{y + 4}{10} = \frac{3}{5}$$

$$\begin{aligned} 5(y + 4) &= 3(10) \\ 5y + 20 &= 30 \end{aligned}$$

$$\begin{aligned} 5y &= 10 \\ y &= 2 \end{aligned}$$

Write the equation of the line in slope-intercept form passing through the given points:

3) $(-2, -3)$ and $(-4, 3)$

$$m = \frac{3 + 3}{-4 + 2} = \frac{6}{-2} = -3$$

$$\begin{aligned} y &= mx + b \\ 3 &= -3(-4) + b \\ 3 &= 12 + b \\ -9 &= b \end{aligned}$$

$$y = -3x - 9$$

4) $(-5, -5)$ and $(-3, -1)$

$$m = \frac{-1 + 5}{-3 + 5} = \frac{4}{2} = 2$$

$$\begin{aligned} y &= mx + b \\ -5 &= 2(-5) + b \\ -5 &= -10 + b \\ 5 &= b \end{aligned}$$

$$y = 2x + 5$$

5) $(5, -7)$ and $(5, 2)$

$$m = \frac{2 + 7}{5 - 5} = \frac{9}{0} = \text{undefined}$$

$$x = 5$$

Write the equation of the line based on the information provided below:

6) parallel to $y = \frac{7}{3}x + 3$; through $(-3, -1)$

$$\begin{aligned} y &= mx + b \\ -1 &= \frac{7}{3}(-3) + b \end{aligned}$$

$$\begin{aligned} -1 &= 7 + b \\ -8 &= b \end{aligned}$$

$$y = -\frac{7}{3}x - 8$$

7) perp. to $y = \frac{1}{2}x + 2$; through $(-3, -7)$

$$\begin{aligned} m &= -2 & y &= mx + b \\ -7 &= -2(-3) + b \end{aligned}$$

$$\begin{aligned} -7 &= 6 + b \\ -13 &= b \end{aligned}$$

$$y = -2x - 13$$

Write the equation of the perpendicular bisector of segment AB:

8) $A(-2, -3), B(-4, 3)$

$$\text{slope of AB} = \frac{3 + 3}{-4 + 2} = \frac{6}{-2} = -3$$

$$\text{midpoint} \left(\frac{-2 + (-4)}{2}, \frac{-3 + 3}{2} \right) \rightarrow (-3, 0)$$

$$\begin{aligned} y &= mx + b \\ 0 &= \frac{1}{3}(-3) + b \\ 0 &= -1 + b \\ 1 &= b \end{aligned}$$

$$y = \frac{1}{3}x + 1$$

9) $A(5, 3), B(-7, 7)$

$$\text{slope of AB} = \frac{7 - 3}{-7 - 5} = \frac{4}{-12} = -\frac{1}{3}$$

$$\text{midpoint} \left(\frac{5 + (-7)}{2}, \frac{3 + 7}{2} \right) \rightarrow (-1, 5)$$

$$\begin{aligned} y &= mx + b \\ 5 &= 3(-1) + b \\ 5 &= -3 + b \\ 8 &= b \end{aligned}$$

$$y = 3x + 8$$

Write the equation of a line that is 1) parallel, 2) coinciding, and 3) intersecting with the line provided.

10) $y = -\frac{7}{3}x + 3$

Parallel: $y = -\frac{7}{3}x + 1$

coinciding: $y = -\frac{7}{3}x + 3$

intersecting: $y = 2x + 1$

↑
same slope↑
same slope
same y-int.

11) $2x + 3y = 12$

↳ $y = -\frac{2}{3}x + 4$

parallel: $y = -\frac{2}{3}x + 1$

coinciding: $y = -\frac{2}{3}x + 4$

↑
intersecting
 $y = 2x + 1$

3.6 Continued

Key

Write the equation of the line that best models the table.

Pick 2 points.

12)

$(x_1, y_1) = (1, -3)$ $(x_2, y_2) = (3, 1)$

13)

$(x_1, y_1) = (7, .45)$ $(x_2, y_2) = (5, .75)$

X	Y
1	-3
3	1
5	5
7	9

$\frac{1+3}{3-1} = \frac{4}{2} = 2 = m$

x	y
3	0.45
5	0.75
7	1.05
10	1.50

$\frac{.75 - .45}{5 - 7} = \frac{.3}{-2} = -.15$

$y = 2x - 5$

$y = mx + b$
 $1 = 2(3) + b$
 $1 = 6 + b$
 $-5 = b$

$y = .15x$

$y = .15x + b$ $b = 0$
 $45 = .15(3) + b$
 $45 = .45 + b$

14) Circle the table that represents the function $y = 4x + 3$?

x	y
0	3
1	4
2	8
3	12

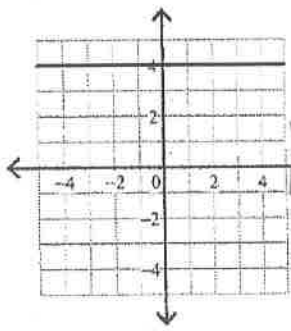
x	y
4	11
5	12
6	13
7	14

x	y
0	3
2	11
4	19
6	27

x	y
1	7
2	11
3	17
4	21

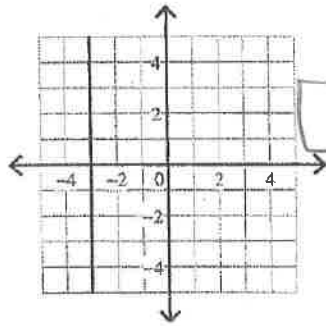
Write the equation of each line.

15.



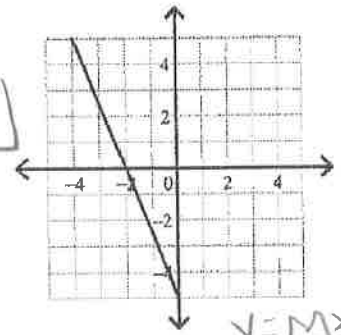
$y = mx + b$
 $y = 4$

16.



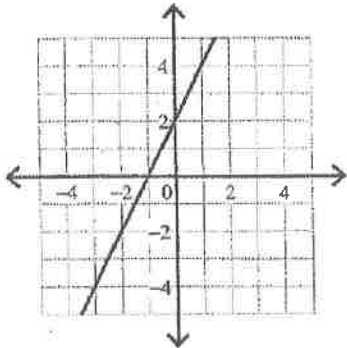
$x = -3$

17.



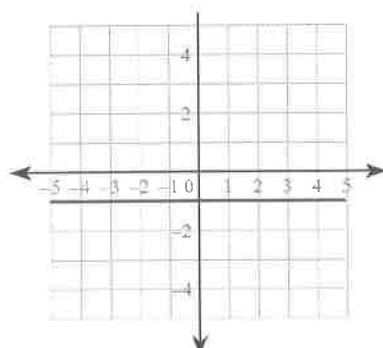
$y = mx + b$
 $y = \frac{5}{2}x - 5$

18.



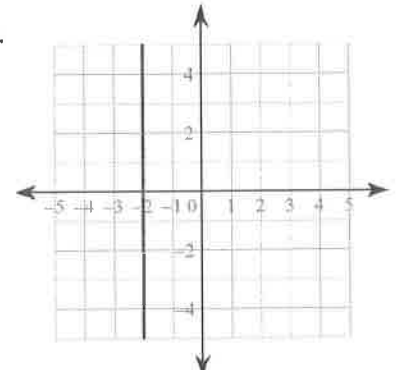
$y = mx + b$
 $y = 2x + 2$

19.



$y = -1$

20.

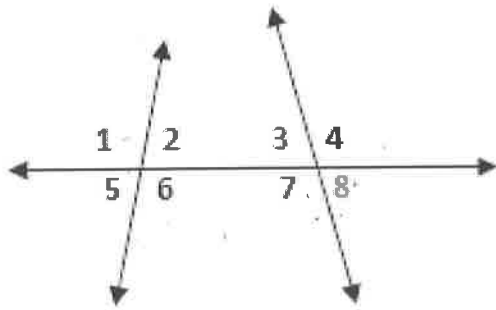


$x = -2$

3.2 - 3.3 - Parallel Lines and Angle Pairs.

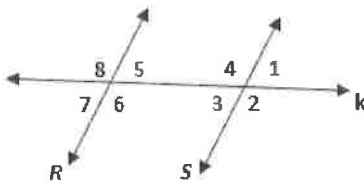
Match the correct angle pair with the given set of angles.

- A. Alternate Interior
- B. Same Side Interior
- C. Alternate Exterior
- D. Corresponding
- E. Vertical
- F. Linear Pair
- G. No Relationship



- 21. $\angle 1, \angle 8$ C
- 22. $\angle 3, \angle 6$ A
- 23. $\angle 3, \angle 7$ F
- 24. $\angle 1, \angle 6$ E
- 25. $\angle 5, \angle 8$ G
- 26. $\angle 2, \angle 4$ D
- 27. $\angle 6, \angle 7$ B

Fill in the Blanks.



by (what theorem?)

- 28. If R is parallel to S, then the corresponding angles are congruent by Corr. \angle 's Postulate.
- 29. If R is parallel to S, then alternate interior angles are congruent by Alt Int \angle 's Thm.
- 30. If R is parallel to S, then same side interior angles are Supplementary by Same Side Int \angle 's Thm.
- 31. If R is parallel to S, then the alternate exterior angles are congruent by Alt. Ext \angle 's Thm.
- 32. If $\angle 2$ and $\angle 6$ are congruent, then R is Parallel to S by Converse of Corr \angle 's Post.
- 33. If $\angle 3$ and $\angle 6$ are Supplementary, then R is Parallel to S by Converse of Same Side Int \angle 's Thm.
- 34. If $\angle 1$ and $\angle 7$ are congruent, then R is Parallel to S by Converse of Alt Ext \angle 's Thm.
- 35. If $\angle 3$ and $\angle 5$ are congruent, then R is Parallel to S by converse of alt int \angle 's Thm.

36. Given $\angle 1 = 4x - 3$ and $\angle 7 = 3x + 4$, find the value of x that makes R and S parallel lines.

$$4x - 3 = 3x + 4$$

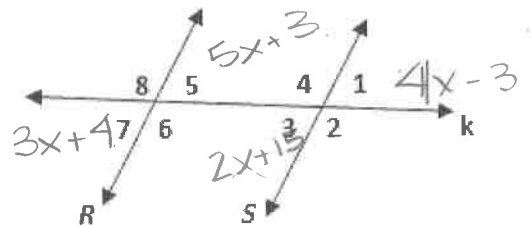
$$+3 \quad +3$$

$$4x = 3x + 7$$

$$-3x \quad -3x$$

$$x = 7$$

$x = 7$



37. If R and S are parallel lines and $\angle 3 = 2x + 15$ and $\angle 5 = 5x + 3$, find the measure of $\angle 2$.

$$2(4) + 15$$

$$8 + 15$$

$$m\angle 3 = 23$$

$$m\angle 2 = 180 - 23$$

$$m\angle 2 = 157^\circ$$

$$2x + 15 = 5x + 3$$

$$-3 \quad -3$$

$$2x + 12 = 5x$$

$$-2x \quad -2x$$

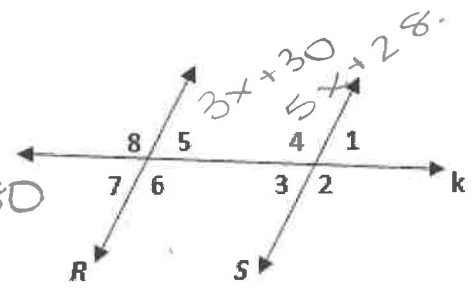
$$12 = 3x$$

$$\frac{12}{3} = \frac{3x}{3}$$

$$4 = x$$

38. If R and S are parallel lines and $\angle 5 = 3x + 30$ and $\angle 4 = 5x + 22$,
find the measure of $\angle 2$.

$$\begin{aligned} 3x + 30 + 5x + 22 &= 180 \\ 8x + 52 &= 180 \\ -52 &\quad -52 \\ \hline 8x &= 128 \\ \frac{8x}{8} &= \frac{128}{8} \quad x = 16 \end{aligned}$$

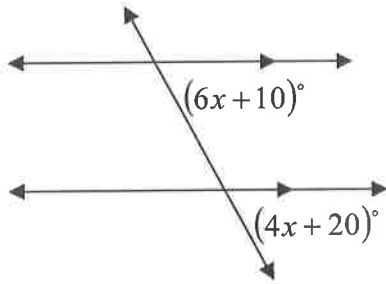


$$m\angle 4 = 5(16) + 22 = 102^\circ$$

$$\boxed{m\angle 2 = m\angle 4 = 102^\circ}$$

Find the value of all missing variables.

39.



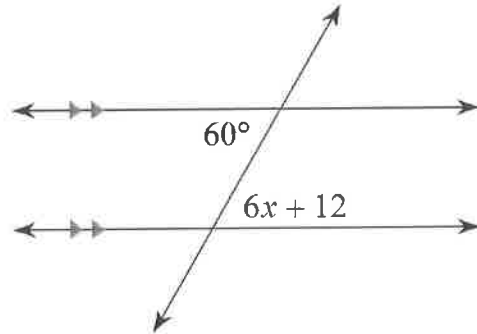
$$\begin{aligned} 6x + 10 &= 4x + 20 \\ -4x &\quad -4x \end{aligned}$$

$$\begin{aligned} 2x + 10 &= 20 \\ -10 &\quad -10 \end{aligned}$$

$$\boxed{x = 5}$$

$$\frac{2x}{2} = \frac{10}{2}$$

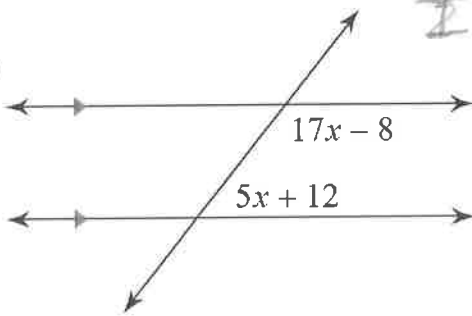
40.



$$\begin{aligned} 60 &= 6x + 12 \\ -12 &\quad -12 \end{aligned}$$

$$\frac{48}{6} = \frac{4x}{4} \quad \boxed{8 = x}$$

41.



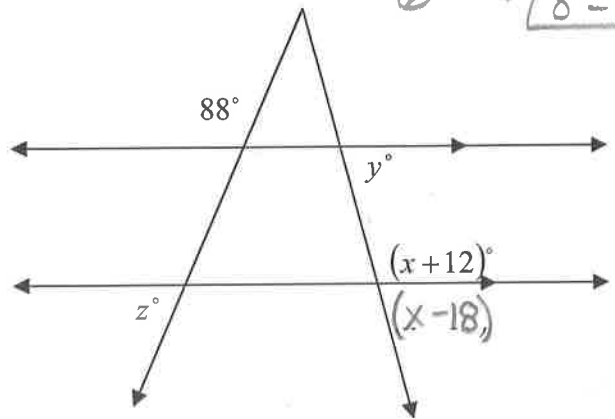
$$17x - 8 + 5x + 12 = 180$$

$$22x + 4 = 180$$

$$\frac{22x}{22} = \frac{176}{22}$$

$$\boxed{x = 8}$$

42.



$$(x + 12) + (x - 18) = 180$$

$$\begin{aligned} 2x - 6 &= 180 \\ +6 &\quad +6 \end{aligned}$$

$$\frac{2x}{2} = \frac{186}{2}$$

$$\boxed{x = 93^\circ}$$

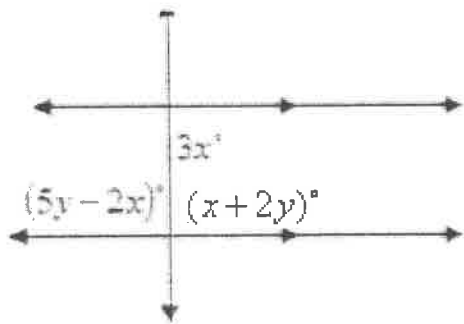
$$y = x - 18$$

$$y = 93 - 18$$

$$\boxed{y = 75^\circ}$$

$$z = 180 - 88$$

$$\boxed{z = 92^\circ}$$



$$\begin{array}{r} 5y - 2x = 3x \\ -3x \quad -3x \\ \hline \end{array}$$

$$\begin{array}{r} 3x + x + 2y = 180 \\ 4x + 2y = 180 \end{array}$$

$$5y - 5x = 0$$

↓ ReArrange

$$-2(-5x + 5y = 0) \rightarrow 10x - 10y = 0$$

$$5(4x + 2y = 180) \rightarrow \frac{20x + 10y = 900}{\frac{30x}{30} = \frac{900}{30}}$$

$$\frac{30x}{30} = \frac{900}{30}$$

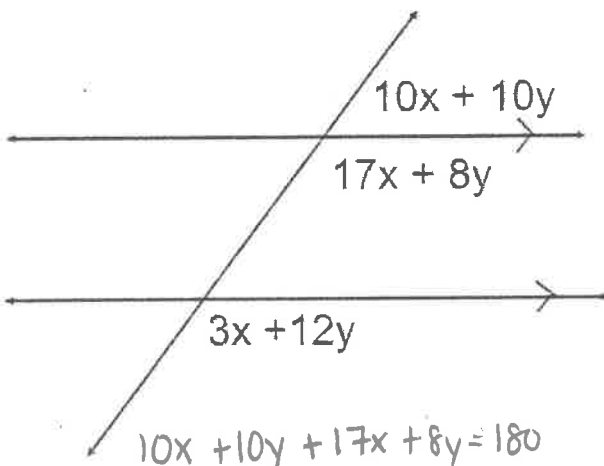
$$\boxed{x = 30}$$

$$4(30) + 2y = 180$$

$$\begin{array}{r} 120 + 2y = 180 \\ -120 \quad -120 \\ \hline \end{array}$$

$$\frac{2y}{2} = \frac{60}{2}$$

$$\boxed{y = 30}$$



$$\begin{array}{r} 17x + 8y = 3x + 12y \\ -3x \quad -3x \\ \hline \end{array}$$

$$\begin{array}{r} 14x + 8y = 12y \\ -12y \quad -12y \\ \hline \end{array}$$

$$14x - 4y = 0$$

$$10x + 10y + 17x + 8y = 180$$

$$27x + 18y = 180$$

$$9(14x - 4y = 0) \rightarrow 126x - 36y = 0$$

$$2(27x + 18y = 180) \rightarrow 54x + 36y = 360$$

$$\frac{180x}{180} = \frac{360}{180}$$

$$\boxed{x = 2}$$

$$14(2) - 4y = 0$$

$$28 - 4y = 0$$

$$-4y = -28$$

$$\boxed{y = 7}$$