

10/10 Algebra - Downing

Warm-up Determine if the relation is a linear function

Ex)

x	y
2	1
5	5
11	13
20	25

 $+3$ (2,1) to (5,5) $+4$ $\frac{4}{3}$
 $+6$ (5,5) to (11,13) $+8$ $\frac{8}{6} = \frac{4}{3}$
 $+9$ (11,13) to (20,25) $+12$ $\frac{12}{9} = \frac{4}{3}$
 All ratios are the same
 Makes it Linear

Ex)

x	y
2	3
4	6
6	12
8	24

Finding slope with 2 points

slope = $\frac{\text{rise}}{\text{run}} = \frac{\text{change in } y}{\text{change in } x}$

slope formula: Given two points (x_1, y_1) (x_2, y_2)

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Ex) $(-10, 10)$ $(-5, 4)$
 x_1, y_1 x_2, y_2

$$m = \frac{4 - 10}{-5 - (-10)} = \frac{-6}{5}$$

Stack Method

Ex) $(-10, 10)$ $(-5, 4)$
 $+5$ \downarrow -6 $m = \frac{-6}{5}$
 or -5 \downarrow $+6$ $m = \frac{6}{-5}$

Ex) $f(8) = 2$ $f(11) = 1$
 $(8, 2)$ $(11, 1)$

$+3$ \downarrow -1
 $m = -\frac{1}{3}$

Ex) $(-2, 7)$ $(-1, 4)$

$+1$ \downarrow -3
 $m = \frac{-3}{1}$

Ex) $f(1) = -2$ $f(2) = -5$
 $(1, -2)$ $(2, -5)$ $+1$ \downarrow -3
 $m = \frac{-3}{1}$

Ex) $f(-2) = 6$ $f(-1) = 3$
 $(-2, 6)$ $(-1, 3)$ $+1$ \downarrow -3
 $m = \frac{-3}{1}$

Writing a linear equation with 2 points

$$y = \boxed{m}x + \boxed{b}$$

\uparrow slope \uparrow y-intercept

Steps	Example
1. Find slope using slope formula or stack method.	$(2, -3)$ and $(4, 1)$ $+2 \begin{matrix} \swarrow (2, -3) \\ \searrow (4, 1) \end{matrix} +4 \quad m = \frac{4}{2} = \boxed{\frac{2}{1}} = 2$
2. Choose a point (x, y)	$(4, 1) \quad m = 2$
3. Using $y = mx + b$ replace $m, x,$ and y	$x \quad y$ $y = mx + b$ $1 = 2(4) + b$ $1 = 8 + b$
4. Solve for b	$-8 \quad -8$ $\hline -7 = b$
5. Using $y = mx + b,$ replace $m + b$	$y = 2x - 7$

Ex) $(12, -3) (14, -4) \quad +2 \begin{matrix} \swarrow (12, -3) \\ \searrow (14, -4) \end{matrix} -1 \quad m = -\frac{1}{2}$

$\begin{matrix} (12, -3) \\ x \quad y \end{matrix}$
 $-3 = -\frac{1}{2}(12) + b$
 $-3 = -6 + b$
 $+6 \quad +6$
 $3 = b$

$y = -\frac{1}{2}x + 3$

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 HW
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 #16-28 Even

Ex) $f(1) = 2 \quad f(3) = 10 \quad +2 \begin{matrix} \swarrow (1, 2) \\ \searrow (3, 10) \end{matrix} +2 \quad m = \frac{12}{2} = 6$

$\begin{matrix} (3, 10) \\ x \quad y \end{matrix}$
 $10 = 6(3) + b$
 $10 = 18 + b$
 $-18 \quad -18$
 $-8 = b$

$y = 6x - 8$