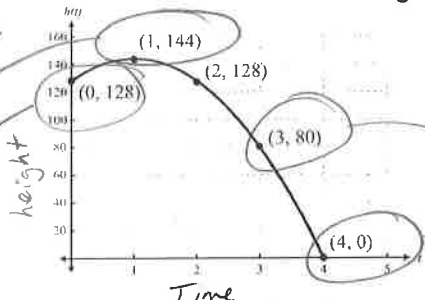


8 Application to Quadratics (day 1).notebook

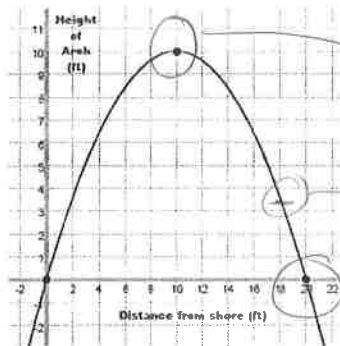
$h(t) \rightarrow$ height
 $t \rightarrow$ time (sec)
 $h(t) = -16t^2 + v_0t + h_0$
 gravity initial vertical velocity initial height

A rock is thrown into a lake from the top of a cliff. The relationship between the height (in feet) of the rock and time (in seconds) after the rock is thrown is illustrated in the graph below.



- a) What is the initial height of the rock? 128 ft.
- b) How high is the rock after 3 seconds? 80 ft.
- c) What is the maximum height of the rock? 144 ft.
- d) How long is the rock in the air? 4 sec.

A golfball is hit from the shoreline of a water hazard. The graph below illustrates the relationship between the height of the golfball and the distance from the shoreline.



- a) What is the height of the golfball when it is 18 ft from the shoreline? 3.5 ft.
- b) If the distance from the shoreline is 10 ft, how high is the golfball? 10 ft.
- c) What is the total horizontal distance the golfball traveled through the air? 20 ft.

A soccer ball is kicked from the ground level with an initial velocity of 32 ft/s. After how many seconds will the ball hit the ground?

$$h(t) = -16t^2 + 32t + 0$$

$$0 = -16t(t - 2)$$

$$\frac{-32t = 0}{-16} \quad t = 0 \quad \frac{t - 2 = 0}{+2} \quad t = 2 \text{ sec}$$

A golf ball is hit from ground level with an initial velocity of 80 ft/s. After how many seconds will the ball hit the ground?

$$h(t) = -16t^2 + 80t + 0$$

$$0 = -16t(t - 5)$$

$$\frac{-80t = 0}{-16} \quad t = 0 \quad \frac{t - 5 = 0}{+5} \quad t = 5 \text{ sec}$$

A football is kicked from ground level with an initial velocity of 48 ft/s.

- a) How long is the ball in the air?
- b) How high is the football after 1.5 seconds?

$$h(t) = -16t^2 + 48t + 0$$

$$0 = -16t(t - 3)$$

$$\frac{-48t = 0}{-16} \quad t = 0 \quad \frac{t - 3 = 0}{+3} \quad t = 3 \text{ sec}$$

Plug in for t

$$h(1.5) = -16(1.5)^2 + 48(1.5)$$

$$h(1.5) = 36 \text{ feet}$$

A stunt woman jumps from a building 73 ft high and lands on an air bag that is 9 ft tall. Her height above ground h in feet can be modeled by $h(t) = 73 - 16t^2$, where t is the time in seconds.

↑ No initial velocity

a) How many seconds will the stunt woman fall before touching the air bag?

b) What is the maximum height of the stunt woman?

73 ft.

$$h(t) = -16t^2 + 73 = 9$$

$$\frac{-16t^2}{-16} = \frac{-64}{-16}$$

$$\sqrt{t^2} = \sqrt{4}$$

$$t = \pm 2$$

2 sec.

The height of a fireworks rocket in meters can be approximated by $h = -5t^2 + 30t$, where h is the height in meters and t is the time in seconds.

a) Find the time it takes the rocket to reach the ground after it has been launched.

b) How high is the firework after 2 seconds?

$$h = -5t^2 + 30t$$

↓ plug in

$$h = -5(2)^2 + 30(2)$$

h = 40 m.

$$0 = -5t(t - 6)$$

$$\frac{-5t}{-5} = \frac{0}{-5} \quad t - 6 = 0$$

$$t = 0$$

$$t = 6 \text{ sec}$$

The height of a diver above the water during a dive can be modeled by $h = -16x^2 + 8x + 48$, where h is the height in feet and x is the time in seconds.

a) What is the initial height of the diver?

48 ft

b) Find the time it takes for the diver to reach the water.

$$h = -16x^2 + 8x + 48$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-8 \pm \sqrt{(8)^2 - 4(-16)(48)}}{2(-16)}$$

$$x = \frac{-8 \pm \sqrt{3136}}{-32}$$

$$\frac{-8 + \sqrt{3136}}{-32} = -1.5$$

$$\frac{-8 - \sqrt{3136}}{-32} = 2 \text{ sec}$$

The height in feet of a soccer ball kicked upward from the ground with initial velocity 60 feet per second is modeled by $h = -16t^2 + 60t$, where t is the time in seconds. Find the time it takes for the ball to return to the ground. Round to the nearest tenth of a second.

$$0 = -16t^2 + 60t$$

$$0 = -4t(4t - 15)$$

$$\frac{-4t}{-4} = \frac{0}{-4}$$

$$t = 0$$

$$4t - 15 = 0$$

$$\frac{4t}{4} = \frac{15}{4}$$

$$t = \frac{15}{4} \text{ or } 3.75 \text{ sec}$$