

7.2 Properties of Parallelograms

Warm Up
Find the value of each variable.

$$29x + 61x = 180$$

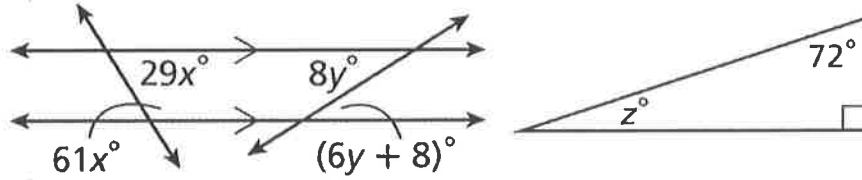
$$90x = 180$$

$$x = 2$$

$$8y = 6y + 8$$

$$2y = 8$$

$$y = 4$$



1. x

2. y

3. z

$$z = 90 - 72$$

$$z = 18$$

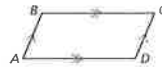
Objectives

Prove and apply properties of parallelograms.

Use properties of parallelograms to solve problems.

Parallelogram a quadrilateral with two pairs of parallel sides

Parallelogram $ABCD$
 $\square ABCD$

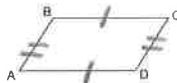


$$\overline{AB} \parallel \overline{CD}, \overline{BC} \parallel \overline{DA}$$

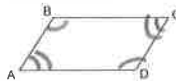
Properties of Parallelograms

If a quadrilateral is a parallelogram, then...

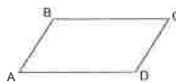
• Opposite sides are congruent
(P-Gram Opposite Sides Thm)



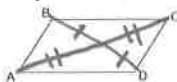
• Opposite angles are congruent
(P-Gram Opposite Angles Thm)



• Consecutive Angles are Supplementary
(P-Gram Consecutive Angles Thm)



• Diagonals Bisect Each Other
(P-Gram Diagonals Thm)



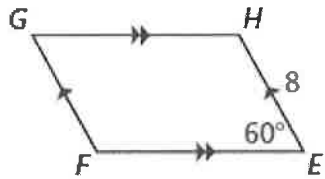
$$m\angle A + m\angle B = 180$$

$$m\angle B + m\angle C = 180$$

$$m\angle C + m\angle D = 180$$

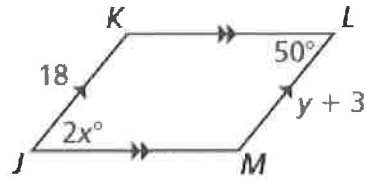
$$m\angle D + m\angle A = 180$$

1. Find FG and $m\angle G$.



$FG = 8$ $m\angle G = 60^\circ$

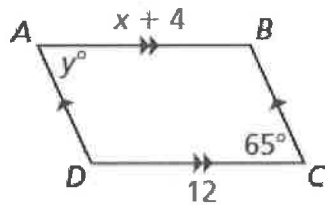
2. Find the values of x and y .



$2x = 50$
 $x = 25$

$y + 3 = 18$
 $y = 15$

3. Find the values of x and y .



$y = 65^\circ$ $x + 4 = 12$
 $x = 8$

Find the coordinates of the intersection of the diagonals of $\square LMNO$ with vertices $L(1, 4)$, $M(7, 4)$, $N(6, 0)$, and $O(0, 0)$. * Diagonals bisect each other, so the midpoints will be the same

mdpt
 $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$

mdpt of LN
 $\left(\frac{1+6}{2}, \frac{4+0}{2}\right) \rightarrow \left(\frac{7}{2}, 2\right)$

mdpt of MO:
 $\left(\frac{7+0}{2}, \frac{4+0}{2}\right) \rightarrow \left(\frac{7}{2}, 2\right)$

Find the coordinates of the intersection of the diagonals of $\square STUV$ with vertices $S(-2, 3)$, $T(1, 5)$, $U(6, 3)$, and $V(3, 1)$.

mdpt of SU:
 $\left(\frac{-2+6}{2}, \frac{3+3}{2}\right) \rightarrow (2, 3)$

mdpt of TV:
 $\left(\frac{1+3}{2}, \frac{5+1}{2}\right) \rightarrow (2, 3)$

Three vertices of $\square ABCD$ are $A(2, 4)$, $B(5, 2)$, and $C(3, -1)$. Find the coordinates of vertex D . $\overline{AB} \parallel \overline{CD}$

slope of AB: $\frac{2-4}{5-2} = -\frac{2}{3}$

D: $(0, 1)$
C: $(3, -1)$

check: slope of AD: $\frac{1-4}{0-2} = \frac{3}{2}$
 $m = \frac{3}{2}$

slope of BC: $\frac{2-(-1)}{3-5} = \frac{3}{-2} = -\frac{3}{2}$
 $m = -\frac{3}{2}$

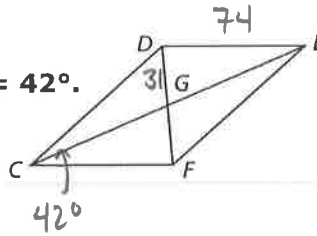
Three vertices of $\square WXYZ$ are $W(-1, -3)$, $X(-3, 2)$, and $Z(4, -4)$. Find the coordinates of vertex Y .

slope of WX: $\frac{2-(-3)}{-3-(-1)} = -\frac{5}{2}$

Z: $(4, -4)$
Y: $(2, 1)$

In $\square CDEF$, $DE = 74$ mm,
 $DG = 31$ mm, and $m\angle FCD = 42^\circ$.
 Find CF .

$$CF = DE = \boxed{74 \text{ mm}}$$



Find $m\angle EFC$.

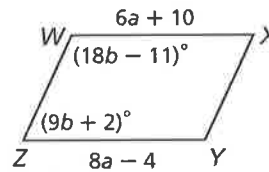
$$m\angle EFC = 180 - 42 = \boxed{138^\circ}$$

Find DF .

$$DF = 2(DG) = 2(31) = \boxed{62}$$

$WXYZ$ is a parallelogram.
 Find YZ .

$$\begin{aligned} 8a - 4 &= 6a + 10 \\ 2a &= 14 \\ a &= 7 \end{aligned} \quad \begin{aligned} YZ &= 8(7) - 4 \\ &= \boxed{52} \end{aligned}$$



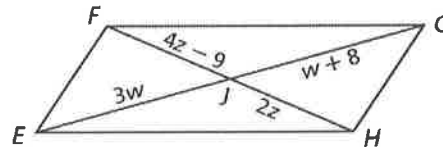
Find $m\angle Z$.

$$\begin{aligned} 9b + 2 + 18b - 11 &= 180 \\ 27b - 9 &= 180 \\ 27b &= 189 \\ b &= 7 \end{aligned} \quad \begin{aligned} m\angle Z &= 9(7) + 2 \\ &= \boxed{65^\circ} \end{aligned}$$

Find JG .

$EFGH$ is a parallelogram.
 Find JG .

$$\begin{aligned} 3w &= w + 8 \\ -w \quad -w \\ \hline 2w &= 8 \\ w &= 4 \end{aligned}$$



$$JG = 4 + 8 = \boxed{12}$$

Find FH .

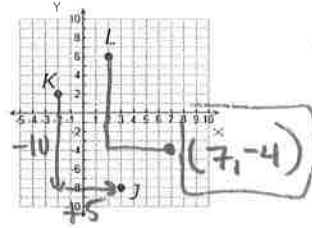
$$\begin{aligned} 4z - 9 &= 2z & JH &= 2(4.5) = 9 \\ -9 &= -2z & FH &= 2(9) = \boxed{18} \\ 4.5 &= z & & \end{aligned}$$

Remember!

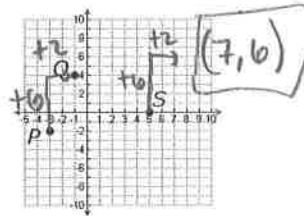
When you are drawing a figure in the coordinate plane, the name $ABCD$ gives the order of the vertices.

Three vertices of JKLM are J(3, -8), K(-2, 2), and L(2, 6). Find the coordinates of vertex M.

Since JKLM is a parallelogram, both pairs of opposite sides must be parallel.



Three vertices of PQRS are P(-3, -2), Q(-1, 4), and S(5, 0). Find the coordinates of vertex R.



Solve for x and y.

$$y = x + 2$$

$$3x = 4y - 10$$

$$3x = 4(x + 2) - 10$$

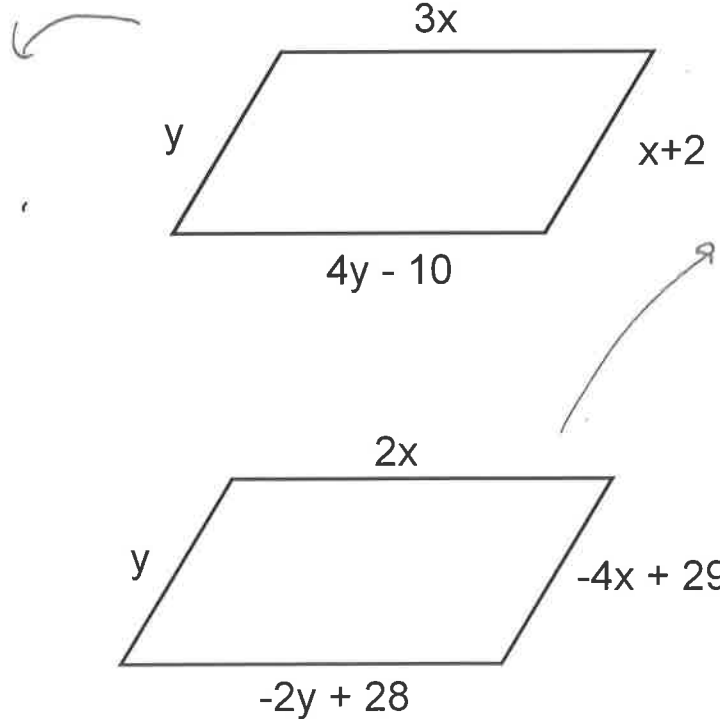
$$3x = 4x + 8 - 10$$

$$-x = -2$$

$$x = 2$$

$$y = (2) + 2$$

$$y = 4$$



$$y = -4x + 29$$

$$2x = -2y + 28$$

$$2x = -2(-4x + 29) + 28$$

$$2x = 8x - 58 + 28$$

$$-6x = -30$$

$$x = 5$$

$$y = -4(5) + 29$$

$$y = 9$$