

WS PC #2 Review Unit 10

Use the information provided to write the standard form equation of each circle.

$$(x-h)^2 + (y-k)^2 = r^2$$

- 1) Center: (-12, 7)
Radius: 3

$$(x+12)^2 + (y-7)^2 = 9$$

- 2) Center: (5, -9)
Radius: 1

$$(x-5)^2 + (y+9)^2 = 1$$

- 3) Center: (16, 2)
Radius: $\sqrt{5}$

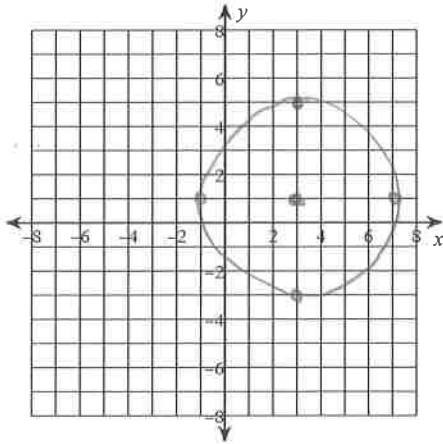
$$(x-16)^2 + (y-2)^2 = 5$$

- 4) Center: (-9, -6)
Radius: 9

$$(x+9)^2 + (y+6)^2 = 81$$

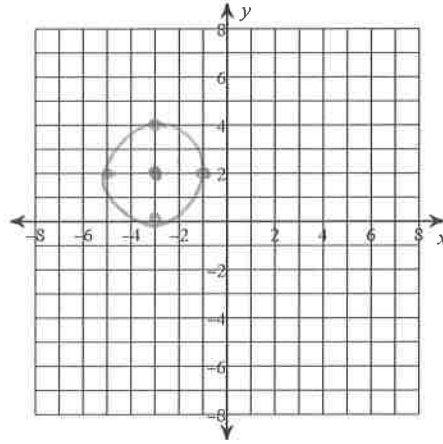
Identify the center and radius of each. Then sketch the graph.

5) $(x-3)^2 + (y-1)^2 = 16$



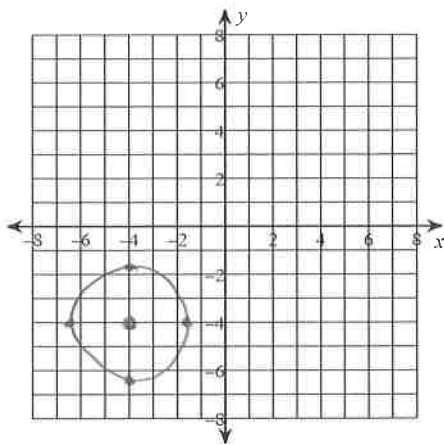
center (3, 1)
r = 4

6) $(x+3)^2 + (y-2)^2 = 9$



center (-3, 2)
r = 3

$$7) x^2 + y^2 + 8x + 8y + 27 = 0$$



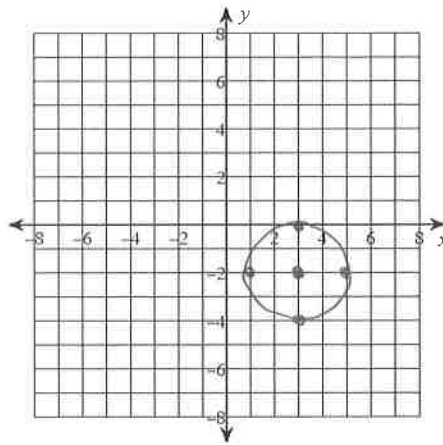
$$x^2 + 8x + \underline{16} + y^2 + 8y + \underline{16} = -27 + \underline{16} + \underline{16}$$

$$(x+4)^2 + (y+4)^2 = 5$$

center $(-4, -4)$

$$r = \sqrt{5}$$

$$8) x^2 + y^2 - 6x + 4y + 9 = 0$$



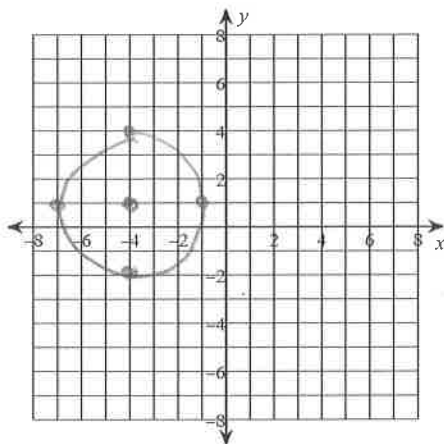
$$x^2 - 6x + \underline{9} + y^2 + 4y + \underline{4} = -9 + \underline{9} + \underline{4}$$

$$(x-3)^2 + (y+2)^2 = 4$$

center $(3, -2)$

$$r = 2$$

$$9) x^2 + y^2 + 8x - 2y + 8 = 0$$



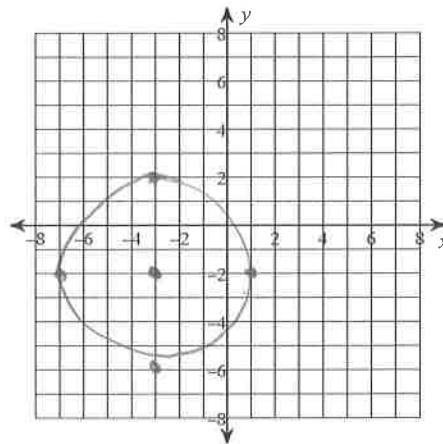
$$x^2 + 8x + \underline{16} + y^2 - 2y + \underline{1} = -8 + \underline{16} + \underline{1}$$

$$(x+4)^2 + (y-1)^2 = 9$$

center $(-4, 1)$

$$r = 3$$

$$10) x^2 + y^2 + 6x + 4y - 3 = 0$$



$$x^2 + 6x + \underline{9} + y^2 + 4y + \underline{4} = 3 + \underline{9} + \underline{4}$$

$$(x+3)^2 + (y+2)^2 = 16$$

center $(-3, -2)$

$$r = 4$$

Write the general form equation of each circle.

11) $x^2 + y^2 - 4x + 8y - 80 = 0$

$$x^2 - 4x + 4 + y^2 + 8y + 16 = 80 + 4 + 16$$

$$(x-2)^2 + (y+4)^2 = 100$$

12) $x^2 + y^2 + 18x - 22y + 197 = 0$

$$x^2 + 18x + 81 + y^2 - 22y + 121 = -197 + 81 + 121$$

$$(x+9)^2 + (y-11)^2 = 5$$

13) $x^2 + y^2 + 32x + 20y + 349 = 0$

$$x^2 + 32x + 256 + y^2 + 20y + 100 = -349 + 256 + 100$$

$$(x+16)^2 + (y+10)^2 = 7$$

14) $x^2 + y^2 - 12x - 6y - 19 = 0$

$$x^2 - 12x + 36 + y^2 - 6y + 9 = 19 + 36 + 9$$

$$(x-6)^2 + (y-3)^2 = 64$$

Solve each equation by factoring.

15) $x^2 - 3x = 40$

$$x^2 - 3x - 40 = 0$$

$$(x-8)(x+5) = 0$$

$$x-8=0 \quad x+5=0$$

$$x = 8, -5$$

16) $5b^2 + 28 = 27b$

$$5b^2 - 27b + 28 = 0$$

$$(5b^2 - 7b)(-20b + 28) = 0$$

$$b(5b-7) - 4(5b-7) = 0$$

$$(b-4)(5b-7) = 0 \quad b-4=0 \quad 5b-7=0$$

$$b = 4, \frac{7}{5}$$

17) $6k^2 = 23k + 35$

$$6k^2 - 23k - 35 = 0$$

$$(6k^2 + 7k)(-30k - 35) = 0$$

$$k(6k+7) - 5(6k+7) = 0$$

$$(k-5)(6k+7) = 0$$

$$k-5=0 \quad 6k+7=0$$

$$k = 5, -\frac{7}{6}$$

18) $21k^2 = 153k + 120$

$$21k^2 - 153k - 120 = 0$$

$$3(7k^2 - 51k - 40) = 0$$

$$(7k^2 + 5k)(-56k - 40) = 0$$

$$k(7k+5) - 8(7k+5) = 0$$

$$(k-8)(7k+5) = 0$$

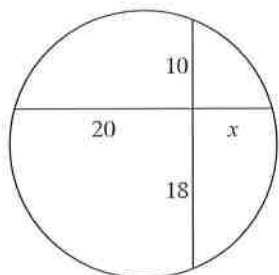
$$k-8=0 \quad 7k+5=0$$

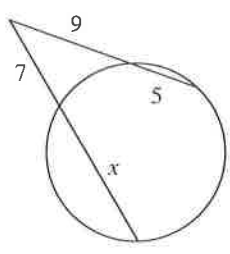
$$k = 8, -\frac{5}{7}$$

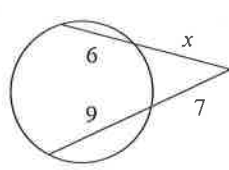
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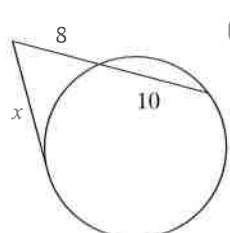
Solve for x. Assume that lines which appear tangent are tangent.

P = Part
O = Outside
W = Whole

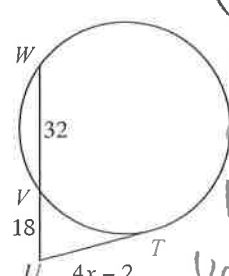
1)  $P \cdot P = P \cdot P$
 $18 \cdot 10 = 20 \cdot x$
 $180 = 20x$
 $x = 9$

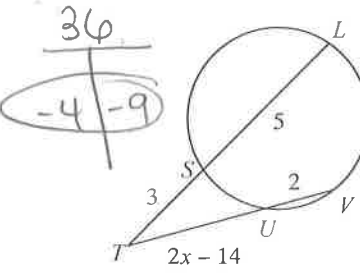
2)  $O \cdot W = O \cdot W$
 $9 \cdot 4 = 7(7+x)$
 $126 = 49 + 7x$
 $77 = 7x$
 $x = 11$

3)  $O \cdot W = O \cdot W$
 $x(x+6) = 7 \cdot 14$
 $x^2 + 6x = 112$
 $x^2 + 6x - 112 = 0$
 $(x^2 - 8x) + (14x - 112) = 0$
 $x(x-8) + 14(x-8) = 0$
 $(x+14)(x-8) = 0$
 $x = 8$

4)  $(\tan)^2 = O \cdot W$
 $x^2 = 8 \cdot 18$
 $x^2 = 144$
 $x = \pm 12$
 $x = 12$

Find the measure of the line segment indicated. Assume that lines which appear tangent are tangent.

5) Find TU $(\tan)^2 = O \cdot W$
 $(4x-2)^2 = 18 \cdot 50$
 $(4x-2)(4x-2)$
 $16x^2 - 16x + 4 = 900$
 $16x^2 - 16x - 896 = 0$
 $16(x^2 - x - 56) = 0$
 $16(x-8)(x+7) = 0$
 $x = 8, -7$
 $x = 8$
 $4(8) - 2 = 30$
 $TU = 30$

6) Find UT $O \cdot W = O \cdot W$
 $2x-14(2x-14+2) = 3 \cdot 8$
 $(2x-14)(2x-12) = 24$
 $4x^2 - 52x + 168 = 24$
 $4x^2 - 52x + 144 = 0$
 $4(x^2 - 13x + 36) = 0$
 $4(x-4)(x-9) = 0$
 $x = 4, 9$
 $2(4) - 14 = -6$
 $2(9) - 14 = 4$
 $UT = 4$